



Department of Local Government Finance

Ratio Study / Trending

2026 Level II Tutorial



Ratio Studies

- Primary tool used to measure mass appraisal performance.
- Compares assessed values to “objectively verifiable data.”
- In our case, compares the assessor’s estimate of TTV to indicators of market value in use.
(i.e. sales prices and/or independent appraisals)



Ratio Studies

- Ratio studies measure certain aspects of assessments:
 - Accuracy – the level of assessment; the overall percentage that TTV represents of market value-in-use.
 - Uniformity – relates to fair and equitable treatment of individual properties; uniformity requires that properties be valued equitably within each major property class, township and that each of these groups be valued at the same level of assessment.
 - Regressivity / Progressivity – relates to whether lower valued properties are under or over-assessed in relation to higher valued properties.



Ratio Studies

- An assessment ratio is calculated using the following formula:
TTV divided by market value = ratio
- Example:

$$\begin{aligned} \text{TTV} &= \$46,500 & \text{Sale Price} &= \$50,000 \\ 46,500 / 50,000 &= .93 \text{ or } 93\% \end{aligned}$$



Ratio Studies

- Let's calculate the assessment ratio on these two sales.
- Sale 1 – sale price is \$218,500; TTV is \$232,400.
- Sale 2 – sale price is \$98,300; TTV is \$96,200.



Ratio Studies

- Let's review the answer to the assessment ratios.
- Sale #1 - $\$232,400 / \$218,500 = 1.064$ or 106.4%.
- Sale #2 - $\$96,200 / \$98,300 = .979$ or 97.9%.



Ratio Studies

- The measures of central tendency are:
 - Median
 - Mean
 - Weighted Mean



Ratio Studies – Median

- The Median is the middle ratio in a rank order of ratios. A rank order lists the ratios in ascending or descending order.



Ratio Studies – Median

- If the sample contains an odd number of sales ratios, the median will be the one which divides the ranked observations into two equal parts.
- If the sample contains an even number of sales ratios, the median will be the arithmetic average of the two ratios in the middle.
- There is a formula for finding the location of the median within the sample once you have ranked the ratios.



Ratio Studies – Median

- The formula is: $n + 1$ divided by 2 = location of the median.
- The letter n represents the number of ratios in the sample.



Ratio Studies – Median

Example with "odd" # of sales

Sales Ratio

0.920
0.920
1.055
0.983
1.075

Median

Ranked Sales Ratios

0.920
0.920
0.983
1.055
1.075

.983 or 98.3%



Ratio Studies – Median

Example with "even" # of sales

Sales Ratio

0.920
0.920
1.055
0.935
0.983
1.075

Ranked Sales Ratios

0.920
0.920
0.935
0.983
1.055
1.075

Median

.959 or 95.9%



Ratio Studies – Median

- The median is affected very little by extreme values because it is based on the ranks of the data – it represents only the middle value.



Problem #1

- Please go to the Ratio Study Problem / Answer packet with Audio and work Problem #1.



Problem #2

- Please go to the Ratio Study Problem / Answer packet with Audio and work Problem #2.



Ratio Studies – Mean & Weighted Mean

- The next things we want to look at are the mean and the weighted mean.
- The mean is the result of adding up all of the ratios and dividing by the number of ratios in the sample.



Ratio Studies – Mean

- The mean is the most common measure of central tendency.
- However, it can be heavily influenced by extreme values.



Ratio Studies – Mean

- Mean (arithmetic average) – The result of adding all the individual ratios and dividing by the number of ratios.
- Mean = sum of ratios ÷ number of ratios

| Sale # | True Tax Value | Sale Price | Sales Ratio |
|------------------------|----------------|------------|-------------|
| 1 | \$ 45,800 | \$ 49,800 | 0.920 |
| 2 | \$ 48,200 | \$ 52,400 | 0.920 |
| 3 | \$ 42,200 | \$ 40,000 | 1.055 |
| 4 | \$ 57,150 | \$ 58,125 | 0.983 |
| 5 | \$ 55,300 | \$ 51,450 | 1.075 |
| Total of Sales Ratios | | | 4.953 |
| Total Number of Ratios | | | 5 |
| Mean | | | 99.05% |

$$4.953 / 5 = .9905 \text{ or } 99.05$$



Ratio Studies – Weighted Mean

- The weighted mean is a measure of central tendency in which each item is adjusted/weighted by a factor reflecting its relative importance to the whole before the items are summed and divided by their number.



Ratio Studies – Weighted Mean

- Weighted Mean – the total of the TTV's for all sales divided by the total of the sales prices for all sales
- Weighted Mean = Sum of the TTV's ÷ Sum of the Sales

| Sale # | True Tax Value | | Sale Price |
|--------|----------------|------------|------------|
| 1 | \$ 45,800 | | \$ 49,800 |
| 2 | \$ 48,200 | | \$ 52,400 |
| 3 | \$ 42,200 | | \$ 40,000 |
| 4 | \$ 57,150 | | \$ 58,125 |
| 5 | \$ 55,300 | | \$ 51,450 |
| | \$ 248,650 | Divided by | \$ 251,775 |

Weighted Mean

.9876 or 98.76%



Problem #3

- Please go to the Ratio Study Problem / Answer packet with Audio and work Problem #3.



Problem #4

- Please go to the Ratio Study Problem / Answer packet with Audio and work Problem #4.



Ratio Studies – Absolute Deviation and Absolute Average Deviation

- The absolute deviation measures the difference between each ratio and the median. Also, the absolute deviation ignores the (+) or (-) differences. (See example on next slide.)
- The absolute average deviation measures the average difference between each ratios and the measure of central tendency.
- Both can be calculated around any measure of central tendency but is usually calculated around the median.



Ratio Study – Absolute Deviation

- When calculating the absolute deviation you need to ignore the (+) or (-) differences of the ratios.

| <u>Sales Ratio</u> | <u>Median</u> | <u>Deviation</u> | <u>Abs Dev</u> |
|--------------------|---------------|------------------|----------------|
| 0.928 | 0.995 | +0.067 | 0.067 |
| 1.013 | 0.995 | -0.018 | 0.018 |



Ratio Studies – Absolute / Average Absolute Deviation

- Example: Absolute Deviation / Average Absolute Deviation Example

| Sale # | True Tax Value | Sale Price | Sales Ratio | Median | Absolute Deviation |
|--------|----------------|------------|----------------------------|--------|--------------------|
| 1 | \$ 45,800 | \$ 49,800 | 0.920 | 0.983 | 0.063 |
| 2 | \$ 48,200 | \$ 52,400 | 0.920 | 0.983 | 0.063 |
| 3 | \$ 42,200 | \$ 40,000 | 1.055 | 0.983 | 0.072 |
| 4 | \$ 57,150 | \$ 58,125 | 0.983 | 0.983 | 0.000 |
| 5 | \$ 55,300 | \$ 51,450 | 1.075 | 0.983 | 0.092 |
| | \$ 248,650 | \$ 251,775 | Total Absolute Deviation | | 0.290 |
| | | | Average Absolute Deviation | | 0.058 |



Ratio Studies – COD

- Coefficient of dispersion – based on the average absolute deviation, but is expressed as a percentage of the measure of central tendency.
 - Most often used with the median.
 - **Calculated by dividing the absolute average deviation by the median and multiplying that answer by 100.**



Ratio Studies – Statistics

Coefficient of Dispersion (COD) =

Ave. Abs. Deviation ÷ Median x 100

| Sale # | True Tax Value | Sale Price | Sales Ratio | Median | Absolute Deviation |
|--------|----------------|------------|----------------------------|--------|---------------------|
| 1 | \$45,800 | \$49,800 | 0.920 | 0.983 | 0.063 |
| 2 | \$48,200 | \$52,400 | 0.920 | 0.983 | 0.063 |
| 3 | \$42,200 | \$40,000 | 1.055 | 0.983 | 0.072 |
| 4 | \$57,150 | \$58,125 | 0.983 | 0.983 | .000 |
| 5 | \$55,300 | \$51,450 | 1.075 | 0.983 | 0.092 |
| | \$248,650 | \$251,775 | Total Absolute Deviation | | 0.290 |
| | | | Average Absolute Deviation | | 0.058 |
| | | | Median | | 0.983 |
| | | | COD | | 5.90% ²⁷ |



Ratio Studies – PRD

- There is one other factor that will need to be taken into account when you work with ratio studies – the price-related differential (PRD).
- The PRD is a statistic that measures assessment regressivity or progressivity.



Ratio Studies – PRD

- Assessments are considered regressive if high value properties are under assessed relative to low value properties.
- Assessments are considered progressive if high value properties are over assessed relative to low value properties.



Ratio Studies – PRD

- PRD is calculated by dividing the mean assessment to sales ratio by the weighted mean ratio.



Ratio Studies – PRD

- Mean = Average of the sales ratios.
- Weighted Mean = Total True Tax Value / Total Sales Price.

| Sale # | True Tax Value | Sale Price | Sales Ratio | |
|--------|----------------|------------|---------------|-------|
| 1 | \$ 45,800 | \$ 49,800 | 0.920 | |
| 2 | \$ 48,200 | \$ 52,400 | 0.920 | |
| 3 | \$ 42,200 | \$ 40,000 | 1.055 | |
| 4 | \$ 57,150 | \$ 58,125 | 0.983 | |
| 5 | \$ 55,300 | \$ 51,450 | 1.075 | |
| | \$ 248,650 | \$ 251,775 | | |
| | | | Mean | .991 |
| | | | Weighted Mean | .988 |
| | | | PRD | 1.003 |
| | | | | |
| | | | | |

PRD = 1.003 or 100.3%



Ratio Studies – Statistics

- **Measures of Regressivity/Progressivity**
- PRD's above 103% tend to indicate assessment regressivity; higher valued properties are under-assessed in relation to lower valued properties.
- PRD's below 98% tend to indicate assessment progressivity; higher valued properties are over-assessed in relation to lower valued properties.



Ratio Study

- Let's review a completed Ratio Study.



Ratio Study – Example

| Sale | TTV | Sales Price | Sales Ratio | Median | Abs Dev |
|----------------|---------|-----------------|---------------|---|---------|
| 1 | 81,900 | 86,000 | 0.952 | 0.958 | 0.006 |
| 2 | 68,900 | 72,000 | 0.957 | 0.958 | 0.001 |
| 3 | 66,200 | 69,000 | 0.959 | 0.958 | 0.001 |
| 4 | 135,200 | 120,000 | 1.127 | 0.958 | 0.169 |
| | | Total Abs. Dev. | | | 0.177 |
| 352,200 | | 347,000 | Avg. Abs. Dev | | 0.0443 |
| | | # of sales | 4 | | |
| | | Mean | 0.999 | (Average of the 4 sales ratios) | |
| | | Median | 0.958 | (Middle sales ratio - Average of .957 & .959) | |
| | | Wghtd. Mean | 1.015 | \$352,200 / \$347,000 | |
| | | COD | 4.624 | Avg. Abs Dev / Median x 100 | |
| | | PRD | 0.984 | Mean / Wghtd. Mean | |



Ratio Study

- Now you will now work a ratio study.
- You will calculate the Sales Ratio, Mean, Median, Absolute Deviation, Average Absolute Deviation, COD, Weighted Mean, & PRD.



Problem #5

- Please go to the Ratio Study Problem / Answer packet with Audio and work Problem #5.



Evaluating Ratio Study Results

- The Annual Adjustments and Equalization Standards Rule sets the following standards:
 1. Accuracy – Median assessment ratio for any class within a township must be between 90% and 110% of TTV.
 2. Uniformity – The coefficient of dispersion for residential improved must be 15% or less and 20% or less for all other classes within a township.
 3. Regressivity/Progressivity – The PRD for any class within a township must be between 98% and 103%.



Level II – Ratio Studies

- This concludes the Ratio Study tutorial and is a reminder that should you have questions you can email these questions to the Department.
- Please send emails to Level2@dlgf.in.gov.